

16 pts.

The Hydrogen Atom

Sol.

1).

$$E_n = \frac{-13.6 \text{ eV}}{n^2}$$

$$\Delta E = E_4 - E_1 = \frac{-13.6 \text{ eV}}{4^2} - \left(\frac{-13.6 \text{ eV}}{1^2} \right) = \boxed{12.8 \text{ eV}}$$

2)

$$E_n = \frac{-13.6 \text{ eV}}{n^2}, \text{ ground state} \rightarrow n=1$$

$$E_1 = -13.6 \text{ eV}$$

$$E_{\text{Final}} = -13.6 \text{ eV} + 12.1 \text{ eV} = -1.5 \text{ eV}$$

- We are now looking for which energy level has the energy of -1.5 eV.

$$E_2 = \frac{-13.6 \text{ eV}}{2^2} = -3.4 \text{ eV}$$

$$E_3 = \frac{-13.6 \text{ eV}}{3^2} = \boxed{-1.5 \text{ eV}} \quad \boxed{n=3}$$

3). Remove electron = ionize

$$\text{ground state: } E_1 = \frac{-13.6 \text{ eV}}{1^2} = -13.6 \text{ eV}$$

$$\Delta E = 0 - (-13.6 \text{ eV}) = \boxed{13.6 \text{ eV}}$$

$$\text{Final state, ionized: } E_{\infty} = \frac{-13.6 \text{ eV}}{\infty^2} \rightarrow 0$$

4. Same method as Q:3 but this time the initial energy level is $n=2$.

$$E_2 = \frac{-13.6 \text{ eV}}{2^2}$$

$$E_\infty = \frac{-13.6 \text{ eV}}{\infty} \rightarrow 0$$

$$\Delta E = 0 - \left(\frac{-13.6 \text{ eV}}{2^2} \right) = \boxed{3.4 \text{ eV}}$$

Matter Waves.

1). $p = \frac{h}{\lambda} \rightarrow \lambda = \frac{h}{p}, \quad p = mv$

$$\lambda = \frac{h}{m v} = \frac{6.6 \times 10^{-34} \text{ J}\cdot\text{s}}{(0.58 \text{ kg})(10 \text{ m/s})} = \boxed{2.2 \times 10^{-36} \text{ m}}$$

$1.32 \times 10^{-34} \text{ m}$

The reason that we don't see the basketball diffract is that its wave length is much smaller than the hoop. For diffraction to occur $\lambda \approx a$ where a is the diameter of the hoop.

2). $\lambda = \frac{h}{p} = \frac{6.6 \times 10^{-34} \text{ J}\cdot\text{s}}{(10^{-4} \text{ kg})(2 \times 10^{-3} \text{ m/s})} = \boxed{3.3 \times 10^{-27} \text{ m}}$

$3.3 \times 10^{-27} \text{ m}$ is 10^{-12} smaller than a proton

3). a. using the de Broglie relation, $P = \frac{h}{\lambda}$

Explanation

→ we need to find the speed (v) of the student such that diffraction will occur. Assume we need the ~~wavelength~~ wavelength of the student to be roughly the same size of the doorway (width).

$$P = \frac{h}{\lambda} \rightarrow mv = \frac{h}{\lambda} \rightarrow v = \frac{h}{m\lambda}$$

$$\lambda \approx 81 \text{ cm} = 81 \times 10^{-2} \text{ m} = 8.1 \times 10^{-1} \text{ m}$$

$$m = 81 \text{ kg}$$

$$v = \frac{6.6 \times 10^{-34} \text{ J}\cdot\text{s}}{(81 \text{ kg}) \cdot (8.1 \times 10^{-1} \text{ m})} = \boxed{1 \times 10^{-35} \text{ m/s}}$$

b). using the speed (v) found above,

$$v = \frac{d}{t} \Rightarrow t = \frac{d}{v}, \quad d = 12 \text{ cm} = 12 \times 10^{-2} \text{ m}$$

$$t = \frac{12 \times 10^{-2} \text{ m}}{1 \times 10^{-35} \text{ m/s}} = \boxed{1.2 \times 10^{34} \text{ s}} \rightarrow \text{a very long time}$$

Just to compare: Age of the universe is $\boxed{4.1 \times 10^{17} \text{ s}} \approx 13 \text{ billion yrs.}$

4). Using $p = \frac{h}{\lambda}$

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

1). $E = 1.0 \text{ eV}$, $E = \frac{p^2}{2m}$

need to convert to Joules 1 eV

$$\frac{1.0 \text{ eV}}{1 \text{ eV}} \left| \frac{1.6 \times 10^{-19} \text{ J}}{\text{eV}} \right. = 1.6 \times 10^{-19} \text{ J}$$

$$p^2 = 2mE \rightarrow p = \sqrt{2mE} = \sqrt{2(9.0 \times 10^{-31} \text{ kg})(1.6 \times 10^{-19} \text{ J})}$$

$$p = 5.4 \times 10^{-25} \text{ kg} \cdot \frac{\text{m}}{\text{s}}$$

$$\lambda = \frac{h}{p} = \frac{6.6 \times 10^{-34} \text{ J} \cdot \text{s}}{5.4 \times 10^{-25} \text{ kg} \cdot \frac{\text{m}}{\text{s}}} = 1.2 \times 10^{-9} \text{ m}$$

$$\boxed{\lambda = 1.2 \text{ nm}}$$

1). $E = 1.0 \text{ keV} = 1.0 \times 10^3 \text{ eV} = 1.6 \times 10^{-16} \text{ J}$

$$p = \sqrt{2 \cdot (9.0 \times 10^{-31} \text{ kg})(1.6 \times 10^{-16} \text{ J})} = 1.7 \times 10^{-23} \text{ kg} \cdot \frac{\text{m}}{\text{s}}$$

$$\lambda = \frac{6.6 \times 10^{-34} \text{ J} \cdot \text{s}}{1.7 \times 10^{-23} \text{ kg} \cdot \frac{\text{m}}{\text{s}}} = 3.9 \times 10^{-11} \text{ m} = 39 \text{ pm}$$